

1. Let  $f(x) = \begin{cases} ax+1 & \text{if } x < 1 \\ 3 & \text{if } x = 1 \\ bx^2+1 & \text{if } x > 1 \end{cases}$ . If  $f(x)$  is continuous at  $x = 1$  then  $(a - b)$  is equal to-

- (A) 0 (B) 1 (C) 2 (D) 4

2. For the function  $f(x) = \frac{1}{x+2\left(\frac{1}{x-2}\right)}$ ,  $x \neq 2$  which of the following holds ?

- (A)  $f(2) = 1/2$  and  $f$  is continuous at  $x = 2$  (B)  $f(2) \neq 0, 1/2$  and  $f$  is continuous at  $x = 2$   
(C)  $f$  can not be continuous at  $x = 2$  (D)  $f(2) = 0$  and  $f$  is continuous at  $x = 2$ .

3. The function  $f(x) = \frac{4-x^2}{4x-x^3}$ , is-

- (A) discontinuous at only one point in its domain.  
(B) discontinuous at two points in its domain.  
(C) discontinuous at three points in its domain.  
(D) continuous everywhere in its domain.

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4. If  $f(x) = \begin{cases} -4\sin x + \cos x & \text{for } x \leq -\frac{\pi}{2} \\ a\sin x + b & \text{for } -\frac{\pi}{2} < x < \frac{\pi}{2} \\ \cos x + 2 & \text{for } x \geq \frac{\pi}{2} \end{cases}$  is continuous then :

- (A)  $a = -1, b = 3$  (B)  $a = 1, b = -3$   
(C)  $a = 1, b = 3$  (D)  $a = -1, b = -3$

5. The function  $f(x) = \begin{cases} \frac{1}{4}(3x^2+1) & -\infty < x \leq 1 \\ 5-4x & 1 < x < 4 \\ 4-x & 4 \leq x < \infty \end{cases}$  is -

- (A) continuous at  $x = 1$  &  $x = 4$   
(B) continuous at  $x = 1$ , discontinuous at  $x = 4$   
(C) continuous at  $x = 4$ , discontinuous at  $x = 1$   
(D) discontinuous at  $x = 1$  &  $x = 4$

6. If  $f(x) = \frac{x^2 - bx + 25}{x^2 - 7x + 10}$  for  $x \neq 5$  and  $f$  is continuous at  $x = 5$ , then  $f(5)$  has the value equal to-

- (A) 0 (B) 5 (C) 10 (D) 25

7. If  $f(x) = \frac{x - e^x + \cos 2x}{x^2}$ ,  $x \neq 0$  is continuous at  $x = 0$ , then -

- (A)  $f(0) = \frac{5}{2}$  (B)  $[f(0)] = -2$  (C)  $\{f(0)\} = -0.5$  (D)  $[f(0)]. \{f(0)\} = -1.5$

where  $[.]$  and  $\{.\}$  denotes greatest integer and fractional part function

8.  $y = f(x)$  is a continuous function such that its graph passes through  $(a, 0)$ . Then  $\lim_{x \rightarrow a} \frac{\log_e(1 + 3f(x))}{2f(x)}$  is-

- (A) 1 (B) 0 (C)  $\frac{3}{2}$  (D)  $\frac{2}{3}$

9. In  $[1, 3]$ , the function  $[x^2 + 1], [.]$  denoting the greatest integer function, is continuous -

- (A) for all  $x$   
(B) for all  $x$  except at nine points  
(C) for all  $x$  except at seven points  
(D) for all  $x$  except at eight points

10. Number of points of discontinuity of  $f(x) = [2x^3 - 5]$  in  $[1, 2]$ , is equal to-

(where  $[x]$  denotes greatest integer less than or equal to  $x$ )

- (A) 14 (B) 13 (C) 10 (D) 8

11. Given  $f(x) = \begin{cases} |x+1| & \text{if } x < -2 \\ 2x+3 & \text{if } -2 \leq x < 0 \\ x^2+3 & \text{if } 0 \leq x < 3 \\ x^3-15 & \text{if } x \geq 3 \end{cases}$ . Then number of point(s) of discontinuity of  $f(x)$  is-

- (A) 0 (B) 1 (C) 2 (D) 3

12. If  $f(x)$  is continuous and  $f\left(\frac{9}{2}\right) = \frac{2}{9}$ , then the value of  $\lim_{x \rightarrow 0} f\left(\frac{1 - \cos 3x}{x^2}\right)$  is-

- (A)  $\frac{2}{9}$  (B)  $\frac{9}{2}$  (C) 0 (D) data insufficient

13.  $f$  is a continuous function on the real line. Given that  $x^2 + (f(x) - 2)x - \sqrt{3} \cdot f(x) + 2\sqrt{3} - 3 = 0$ . Then the value of  $f(\sqrt{3})$

- (A) can not be determined (B) is  $2(1 - \sqrt{3})$   
(C) is zero (D) is  $\frac{2(\sqrt{3} - 2)}{\sqrt{3}}$

14. The function  $f(x) = [x]^2 - [x^2]$  (where  $[y]$  is the greatest integer less than or equal to  $y$ ), is discontinuous at:

- (A) all integers (B) all integers except 0 & 1  
(C) all integers except 0 (D) all integers except 1